| A satellite moves in a circular orbit of radius 15 300 km from the centre of the | e Earth.                    |
|--|-----------------------------|
| (i) State one of the main benefits satellites have on our lives.                 |                             |
|  | P41                         |
| (ii) Calculate the gravitational field strength g at the radius of 15 300 km.    |                             |
|  |                             |
|  |                             |
|  |                             |
|  | 4                           |
|  | g =  N kg <sup>-1</sup> [2] |
| (iii) Calculate the period of the orbiting satellite.                            |                             |
|  |                             |
|  |                             |
|  |                             |
|  | period = s [3]              |
|  |                             |
|  |                             |
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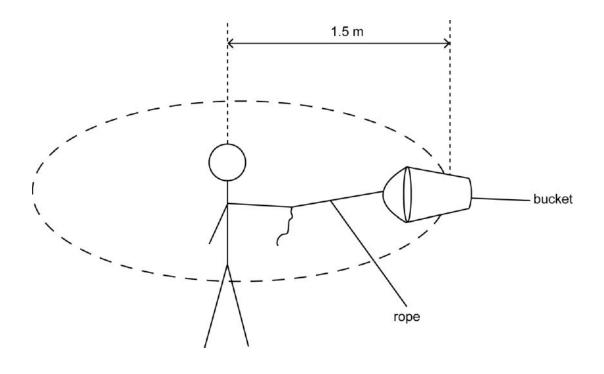
1

2(a) For a mass m moving at constant speed v in a circle of radius r, the expression for the centripetal force F is

$$F = \frac{mv^2}{r}$$

| Explain the term centripetal force. |    |   |
|-------------------------------------|----|---|
|                                     |    |   |
|                                     | [1 | 1 |

(b) A rope is attached to a bucket. A man swings the bucket in a horizontal circle of radius 1.5 m. The bucket has a constant speed of 4.8 m s<sup>-1</sup>. The mass of the bucket is 5.0 kg.



(i) Calculate the tension F in the rope.

(ii) Calculate the angular velocity  $\boldsymbol{\omega}$  of the rotating bucket.

$$\omega =$$
\_\_\_\_\_ rad s<sup>-1</sup> [2]

| (c) | * A student wishes to test the equation $F = \frac{mv^2}{r}$ for a constant force $F$ using a whirling bung in the laboratory.   |
|-----|--|
|     | Describe with the aid of a labelled diagram how an experiment can be conducted, and how the data can be analysed to test the validity of this equation for a constant force. |
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3(a) Fig. 2.1 shows the circular path described by a helium nucleus in a region of uniform magnetic field in a vacuum.

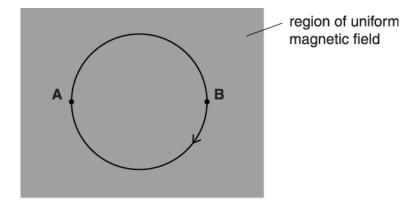


Fig. 2.1

The direction of the magnetic field is perpendicular to the plane of the paper. The magnetic flux density of the magnetic field is 0.20 mT. The radius of the circular path is 15 cm. The helium nucleus has charge  $+ 3.2 \times 10^{-19}$  C and mass  $6.6 \times 10^{-27}$  kg.

Explain why the helium nucleus

| (i)  | travels in a circular path                             |         |
|------|--|---------|
|      |  | <br>[1] |
| (ii) | has the same kinetic energy at <b>A</b> and <b>B</b> . | 4-1     |
|      |  |         |
|      |  | <br>[1] |

|     | ww   | w.quantumvisionacademy.com |
|-----|--|----------------------------|
| (b) | ) Calculate the magnitude of the momentum of the helium nucleus. |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     |  |                            |
|     | momentum =   | kg m s <sup>-1</sup> [3]   |
|     |  |                            |
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Fig. 3.1 shows a simple pendulum consisting of a steel sphere suspended by a light string from a rigid support. The sphere is displaced 50 mm from its vertical equilibrium position and released at time t = 0.

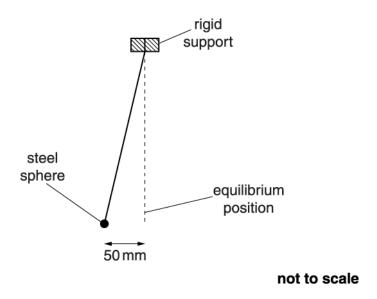
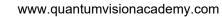


Fig. 3.1

Fig. 3.2 shows the graph of displacement *x* of the sphere against time *t*.



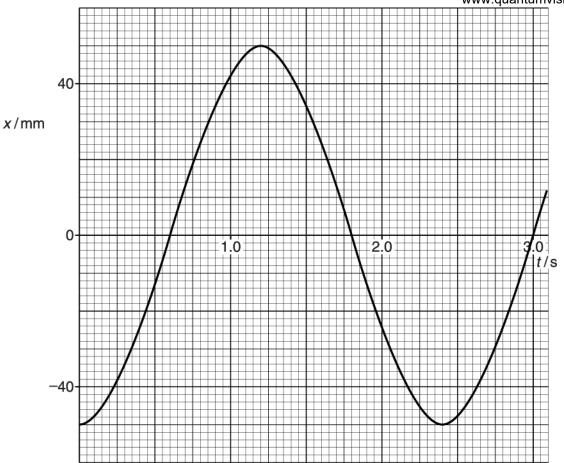


Fig. 3.2

The sphere is released from rest with a displacement x = 25 mm. State with a reason, the change if any in

| (i)  | the frequency of the oscillations         |
|------|---|
|      |   |
|      |   |
|      |   |
|      | [1]                                       |
| (ii) | the maximum kinetic energy of the sphere. |
|      |   |
|      |   |
|      |   |
|      |   |

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|------------------------------|
| [2]                          |

5(a) Fig. 22.1 shows the circular track of a positron moving in a uniform magnetic field.

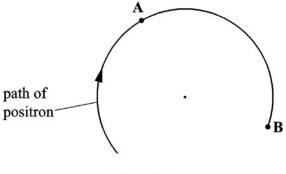


Fig. 22.1

The magnetic field is perpendicular to the plane of Fig. 22.1.

The speed of the positron is  $5.0 \times 10^7 \ m \ s^{-1}$  and the radius of the track is 0.018 m.

| State the direction the speed of the p |            | sitron when at point <b>A</b> and e | xplain why this force does <b>not</b> | change |
|--|------------|-------------------------------------|---------------------------------------|--------|
| the speed of the p                     | 005111011. |                                     |                                       |        |
|  |            |                                     |                                       |        |
|  |            |                                     |                                       |        |
|  |            |                                     |                                       | [2]    |
|  |            |                                     |                                       |        |

(b) Calculate the magnitude of the magnetic flux density of the magnetic field.

magnetic flux density = \_\_\_\_\_ T [3]

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|---|---|
| 6 | Fluorodeoxyglucose (FDG) is a radioactive tracer often used for PET scans. It contains radioactive fluorine-18, |
|   | which is a positron-emitter. Some information about FDG and fluorine-18 is given below.                         |
|   |   |
|   |   |
|   | • 9.9% of the mass of FDG is fluorine-18.   |
|   | The half-life of fluorine-18 is 6600 s.   |
|   | <ul> <li>The molar mass of fluorine-18 is 0.018 kg mol<sup>-1</sup>.</li> </ul>                                 |

A patient is injected with FDG. The initial activity of FDG is 400 MBq.

Use the information given to calculate the initial mass of FDG given to the patient.

| mass = | = |      |      |      | kg | <b>Γ</b> 41 |  |
|--------|---|------|------|------|----|-------------|--|
| mass   |   | <br> | <br> | <br> | ng | נייו        |  |

7(a) An astronomer uses a spectrometer and diffraction grating to view a hydrogen emission spectrum from a star.

The light is incident normally on the grating.

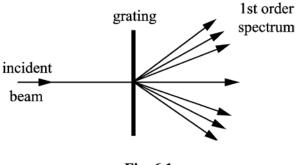


Fig. 6.1

First order diffraction maxima are observed at angles of 12.5°, 14.0° and 19.0° to the direction of the incident light as shown in **Fig. 6.1**.

Two of the wavelengths are  $4.33 \times 10^{-7}$  m and  $4.84 \times 10^{-7}$  m.

Calculate the wavelength of the third line.

| wavelength = m  2 | wavelength = |  |  |  | m [2 |
|-------------------|--------------|--|--|--|------|
|-------------------|--------------|--|--|--|------|

- (b) In order to increase the accuracy of the values for wavelength, the student decides to look for higher order diffraction maxima.
  - (i) State how this increases the accuracy.

| <br> | <br>    |
|------|---------|
| <br> | <br>[1] |

(ii) Calculate how many orders n can be observed for the shorter wavelength given in (a).

| c) |      | ese three emission lines all arise from transitions agram of hydrogen relevant to these transitions is | ns to the same final energy level. The part of the energy level is shown in Fig. 6.2. |
|----|------|--|---|
|    |      |  |   |
|    |      |  |   |
|    |      |  | Fig. 6.2  |
|    | (i)  | Draw lines between the energy levels to indicate label them with their wavelengths.                    | ate the transitions which cause the three emission lines and                          |
|    |      |  | [1  |
|    | (ii) | There are other possible transitions between the these produces photons of $4.8 \times 10^{-20}$ J.    | he energy levels shown in Fig. 6.2. The least energetic of                            |
|    |      | Calculate the wavelength of these photons.   |   |
|    |      | State in which region of the electromagnetic sp  | pectrum this wavelength is found.   |
|    |      |  |   |
|    |      |  |   |
|    |      |  | wavelength n  |
|    |      |  |   |
|    |      |  | region:[3   |
|    |      |  |   |

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|------|--|------------------------------|
| 8(a) | The International Space Station (ISS) circles the Earth at a height      |                              |
|      | Its mass is $4.2 \times 10^5$ kg.  |                              |
|      | The radius of the Earth is $6.4 \times 10^6$ m.                          |                              |
|      |  |                              |
|      | (i) Show that the speed of the ISS in orbit is about 8 km $\rm s^{-1}$ . |                              |
|      |  |                              |
|      |  |                              |
|      |  |                              |
|      |  | [3]                          |
|      | (ii) Calculate the total energy of the ISS.                              | [9]                          |
|      | (, , , , , , , , , , , , , , , , , , ,                                   |                              |
|      |  |                              |
|      |  | total energy = J [2]         |
|      |  |                              |
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|--------------|--|------|
| (b)          |  |      |
|              | circular orbit above the Earth and at the same speed as the ISS. The two craft are separated by a distance of  | a    |
|              | few kilometres. The rocket is behind the ISS. It can move closer to the ISS using the following procedure.   |      |
|              |  |      |
|              | The rocket engines are fired in reverse for a few seconds to slow the rocket down. This action causes the rocket   | cket |
|              | to fall into an orbit nearer to the Earth.   |      |
|              |  |      |
|              | After an appropriate time, the rocket engines are fired forwards for a few seconds to move the rocket back in  | to   |
|              | the original orbit closer to the ISS.  |      |
|              |  |      |
|              | Use your knowledge of gravitational forces and uniform motion in a circular orbit to explain the physics of this   | 3    |
|              | procedure.   |      |
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|              |  | [6]  |
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9(a) Fig. 11.1 shows a diagram of Andromeda, our nearest galaxy.

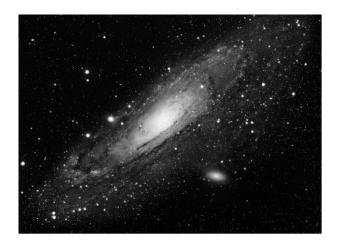


Fig. 11.1

Andromeda is  $2.4 \times 10^{22}$  m from the Earth. It has a diameter of  $1.3 \times 10^{20}$  m.

All the stars in Andromeda rotate about its centre. Some stars in Andromeda are moving towards us and some are moving away from us. The outermost stars in Andromeda have a rotational speed of  $2.5 \times 10^5$  m s<sup>-1</sup>. The wavelength of the hydrogen-alpha spectral line in the laboratory is 656.3 nm. The wavelength of this spectral line from the outermost stars is Doppler shifted when observed from the Earth. Calculate the change in wavelength of this spectral line due to this rotation.

change in wavelength = \_\_\_\_\_ nm [2]

| (b) | The circular motion of the outermost stars is due to the gravitational attraction of all the stars in Andromeda. Assume that the mass of Andromeda providing the gravitational force on these outermost stars is all at the entre of this galaxy.  The average mass of a star is 2.0 × 10 <sup>30</sup> kg.  Estimate the total number of stars in Andromeda. |
|-----|---|
|     | number of stars =[4   |
| 10  | The Earth takes 1 day to rotate once about its axis.  What is the angular velocity of a point on the surface of the Earth?  |
|     | 2.0 × $10^{-7}$ rad s <sup>-1</sup><br>7.3 × $10^{-5}$ rad s <sup>-1</sup><br>4.4 × $10^{-3}$ rad s <sup>-1</sup><br>2.6 × $10^{-1}$ rad s <sup>-1</sup>  |
|     |   |

[1]

Your answer

| 1 1 | An object of mass <i>m</i> is attached to a string and then whirled in a horizontal circle. The speed of the object is |
|-----|--|
|     | slowly increased from zero. The string breaks when the object has a maximum speed of 1.00 m s <sup>-1</sup> .          |
|     | The experiment is repeated with an identical string but with an object of mass $1.5\ m$ . The radius of the circle is  |
|     | kept constant.   |

What is the maximum speed of this object when the string breaks?

| Α | $0.67 \text{ m s}^{-1}$ |
|---|-------------------------|
| В | $0.82 \text{ m s}^{-1}$ |
| С | $1.22 \text{ m s}^{-1}$ |
| D | $1.50 \text{ m s}^{-1}$ |
|   |                         |

| Valur analyar |  |
|---------------|--|
| Your answer   |  |
|               |  |

[1]

[2]

12(a) Fig. 2.1 shows a jet aircraft preparing for take-off along a horizontal runway. The engine of the jet is running but the brakes are applied. The jet is not yet moving.



Fig. 2.1

On Fig. 2.1 draw an arrow to show each of the following forces acting on the jet:

- (ii) the force produced by the engine (label this T)
- (iii) the **total** force exerted by the runway on the jet (label this **F**).

(b) The brakes are released. A jet plane is taking off. The maximum force produced by the engine is 28 kN. The take-off speed of the jet is  $56 \text{ m s}^{-1}$ . The mass of the jet is 6200 kg.

(i) Calculate the minimum distance the jet travels from rest to the point where it takes off.

distance = \_\_\_\_ m [3]

(ii) Explain why the runway needs to be longer than the distance calculated in (i).

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(c) The A jet is to be used in a flying display in which the pilot will be required to fly the jet in a **horizontal** circle of radius *r*, at a constant speed of 86 m s<sup>-1</sup>. This is achieved by flying the jet with its wings at 35° to the horizontal. With the jet flying in this way, the two forces acting on the jet are the lift *L* and the weight *W*, as shown in Fig. 2.2. Air resistance has negligible effect on the motion of the jet during this manoeuvre.

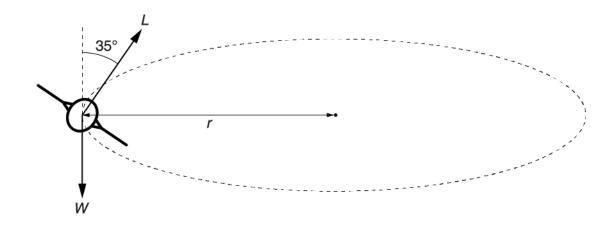


Fig. 2.2

(i) Show that the magnitude of the force L is about 74 kN.

| _[1] |
|------|
|      |

(ii) Calculate the radius r.

(d) In a more complex manoeuvre (loop the loop), the a pilot is required to fly in a vertical circle at a constant speed as shown in Fig. 2.3.

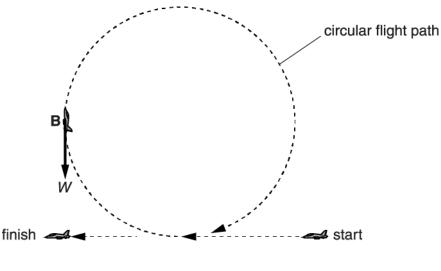


Fig. 2.3

- (i) For a certain speed, the pilot can experience a sensation of weightlessness at a particular point along the circular path.
  - 1 On Fig. 2.3, mark with a cross labelled **A**, the point where the pilot experiences the sensation of weightlessness.

[1]

2 State the magnitude of the vertical component of the contact force exerted by the seat on the pilot at A.

force = \_\_\_\_\_ N [1]

- (ii) In this manoeuvre it is convenient to analyse the motion of the jet in terms of two forces:
  - ∘ a constant weight W
  - ∘ a variable force *P*.

*P* is the resultant of the engine thrust, the lift from the wings and air resistance.

At the point **B** in Fig. 2.3 the jet is flying vertically upwards.

Explain why the force *P* is not directed towards the centre of the circular path.

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|------------------------------|
| <br>                         |
|                              |
| <br>[1]                      |
|                              |

13(a) This question is about the motion of a ball suspended by an elastic string above a bench. The mass of the string is negligible compared to that of the ball. Ignore air resistance.



Fig. 6.1

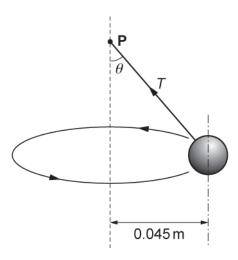


Fig. 6.2 (not to scale)

In Fig. 6.1 the ball of weight 1.2 N hangs vertically at rest from a point P. The extension of the string is 0.050 m. The string obeys Hooke's law.

In Fig. 6.2 the ball is moving in a horizontal circle of radius 0.045 m around a vertical axis through **P** with a period of 0.67 s. The string is at an angle  $\theta$  to the vertical. The tension in the string is T.

On Fig. 6.2 draw and label one other force acting on the ball.

[1]

| (b) |
|-----|
|-----|

| (i) Resolve the tension $T$ horizontally and vertically and show that the angle $\theta$ is 22°. |     |
|--|-----|
|  |     |
|  |     |
|  |     |
|  | [2] |
| (ii) Calculate the extension <i>x</i> of the string shown in Fig. 6.2.                           |     |
|  |     |

x = \_\_\_\_ m [3]

(c) Whilst rotating in the horizontal plane the ball suddenly becomes detached from the string. The bottom of the ball is 0.18 m above the bench at this instant. The ball falls as a projectile towards the bench beneath. Fig. 6.3 shows the view from above.

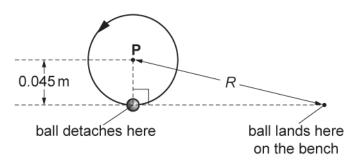


Fig. 6.3

Calculate the horizontal distance *R* from the point on the bench vertically below the point **P** to the point where the ball lands on the bench.

| R=  |  |  |  | m | [4] |
|-----|--|--|--|---|-----|
| , , |  |  |  |   | . – |

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| (d) | Returning to the situation shown in Fig. 6.2, state and explain what happens when the rate of rotation of the ball is increased. |
|-----|--|
|     |  |
|     |  |
|     |  |
|     |  |
|     | [2]  |
|     | <del>-</del> -   |

Phobos is one of the two moons orbiting Mars. Fig. 17.1 shows Phobos and Mars.

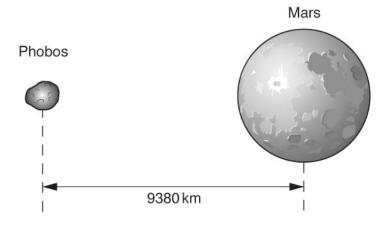


Fig. 17.1

The orbit of Phobos may be assumed to be a circle. The centre of Phobos is at a distance 9380 km from the centre of Mars and it has an orbital speed  $2.14 \times 10^3$  m s<sup>-1</sup>.

- (i) On Fig. 17.1, draw an arrow to show the direction of the force which keeps Phobos in its orbit. [1]
- (ii) Calculate the orbital period *T* of Phobos.

(iii) Calculate the mass *M* of Mars.

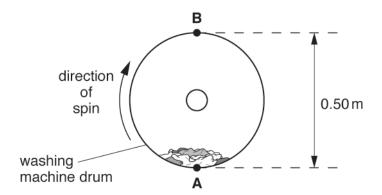


Fig. 21

The clothes inside the drum are spun in a vertical circular motion in a clockwise direction.

The drum has diameter 0.50 m. The manufacturer of the washing machine claims that the drum spins at  $1600 \pm 100$  revolutions per minute.

Calculate the speed of rotation of the drum and the absolute uncertainty in this value.

| drum at point B start to drop off at a certain speed v.              | he |
|--|----|
| At this speed $v$ , the normal contact force on the clothes is zero. |    |
| Calculate the speed v.   |    |
|  |    |
|  |    |
|  |    |
|  |    |
| V= ms <sup>-1</sup> [3   | 3] |
|  |    |

16 A binary star is a pair of stars which move in circular orbits around their common centre of mass.

In this question consider the stars to be point masses situated at their centres.

Fig. 3.1 shows a binary star where the mass of each star is *m*. The stars move in the same circular orbit.

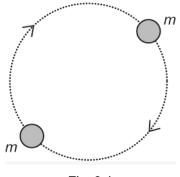


Fig. 3.1

|   | [2  |
|---|---|
|   |   |
|   |   |
|   |   |
|   |   |
| ) | Explain why the stars of equal mass must always be diametrically opposite as they travel in the circular orbit. |

| (ii) | The centres of the two stars are separated by a distance of $2R$ equal to $3.6 \times 10^{10}$ m, where $R$ is the radiu |
|------|--|
|      | of the orbit. The stars have an orbital period T of 20.5 days. The mass of each star is given by the equatio             |

$$m = \frac{16\pi^2 R^3}{GT^2}$$

where G is the gravitational constant.

Calculate the mass m of each star in terms of the mass  $M_{\odot}$  of the Sun.

1 day = 86400 s  
$$M_{\odot}$$
 = 2.0 × 10<sup>30</sup> kg



- (iii) The stars are viewed from Earth in the plane of rotation.
  - The stars are observed using light that has wavelength of 656 nm in the laboratory. The observed light from the stars is Doppler shifted.

Calculate the maximum change in the observed wavelength  $\Delta\lambda$  of this light from the orbiting stars. Give your answer in nm.

At an airport, the conveyor belt for suitcases moves at a constant speed of 1.5 m s<sup>-1</sup>. In Fig. 4.1, a suitcase of mass 8.0 kg has reached the line labelled XX'.

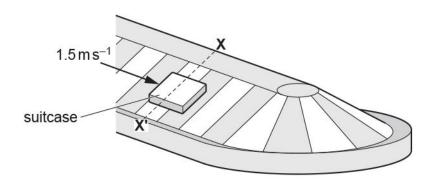


Fig. 4.1

Fig. 4.2 shows the situation in vertical cross-section. The frictional force F prevents the suitcase of weight W from sliding to the bottom of the belt.

The normal contact force on the suitcase is *R*.

The belt is inclined at an angle of 30° to the horizontal.

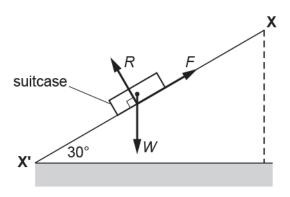


Fig. 4.2 (not to scale)

Fig. 4.3 shows the suitcase and the forces acting on it at the line labelled YY'.

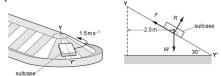


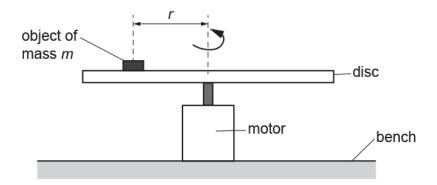
Fig. 4.3

The centre of mass of the suitcase is now moving at  $1.5 \text{ m s}^{-1}$  along a semi-circular arc of radius 2.0 m.

(i) Calculate the magnitude of the centripetal force acting on the suitcase.

|      | centripetal force = N [2]   |
|------|---|
| (ii) | When the suitcase is at line $YY'$ , the magnitude of force $F$ is larger and the magnitude of force $R$ is smaller than at $XX'$ . |
|      | Explain why this is so.   |
|      |   |
|      |   |
|      |   |
|      |   |
|      |   |
|      |   |
|      |   |
|      |   |
|      |   |
|      | [4]   |

18(a) A small object of mass m is placed on a rotating horizontal metal disc at a distance r from the centre of the disc.



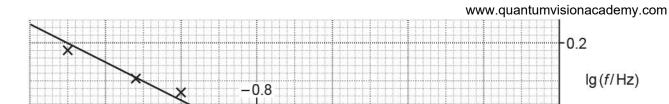
The frequency of rotation is adjusted using a motor attached to the disc.

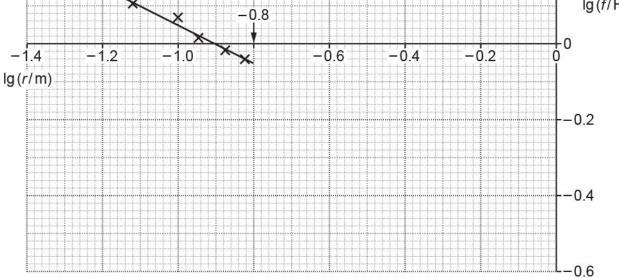
The frequency of rotation of the disc is slowly increased from zero, until the object slips off. At this point, the friction *F* acting on the object is equal to the centripetal force.

The friction F is given by the expression F = kmg, where k is a constant and g is the acceleration of free fall. The constant k has no units.

Show that the frequency f at which the object slips off is given by the equation  $f^2 = \left(\frac{gk}{4\pi^2}\right) \times \frac{1}{r}$ .

(b) A student plots a graph of  $\lg (f/Hz)$  against  $\lg (r/m)$ .





For this graph: *y*-intercept =  $\frac{1}{2} \times \lg \left( \frac{gk}{4\pi^2} \right)$ 

Use the graph to determine the constant *k*. Write your answer to 2 significant figures.

| 19(a | )The International Space Station (ISS) orbits the Earth at a height of 4.1 × 10° m <b>above</b> the Earth's surface.                         |
|------|--|
|      | The radius of the Earth is $6.37 \times 10^6$ m. The gravitational field strength $g_0$ at the Earth's surface is $9.81 \text{ N kg}^{-1}$ . |
|      | Both the ISS and the astronauts inside it are in free fall.  |
|      | Explain why this makes the astronauts feel weightless.   |
|      |  |
|      |  |
|      |  |
|      | [1]  |
| (b)  |  |
|      | (i) Calculate the value of the gravitational field strength $g$ at the height of the ISS above the Earth.                                    |
|      |  |
|      |  |
|      |  |
|      | g =  |
|      |  |
|      | (ii) The speed of the ISS in its orbit is 7.7 km s <sup>-1</sup> . Show that the period of the ISS in its orbit is about 90 minutes.         |
|      |  |
|      |  |
|      |  |
|      | [2]  |
|      |  |
|      |  |
|      |  |
|      |  |

- (c) Use the information in **(b)(ii)** and the data below to show that the root mean square (r.m.s.) speed of the air molecules inside the ISS is approximately 15 times smaller than the orbital speed of the ISS.
  - molar mass of air =  $2.9 \times 10^{-2} \text{ kg mol}^{-1}$
  - temperature of air inside the ISS = 20 °C

[3]

(d) The ISS has arrays of solar cells on its wings. These solar cells charge batteries which power the ISS. The wings always face the Sun.

Use the data below and your answer to (b)(ii) to calculate the average power delivered to the batteries.

- The total area of the cells facing the solar radiation is 2500 m<sup>2</sup>.
- 7% of the energy of the sunlight incident on the cells is stored in the batteries.
- The intensity of solar radiation at the orbit of the ISS is 1.4 kW m<sup>-2</sup> outside of the Earth's shadow and zero inside it.
- The ISS passes through the Earth's shadow for 35 minutes during each orbit.

| average power = |  | W | [· | 4 | ŀ] |
|-----------------|--|---|----|---|----|
|-----------------|--|---|----|---|----|

# **END OF QUESTION PAPER**

| Q | Question |     | Answer/Indicative content  | Marks | Guidance   |  |
|---|----------|-----|--|-------|--|--|
| 1 |          | i   | Any sensible suggestion, e.g. Satellites used for global communication, instant access to news, weather forecasting etc. | B1    |  |  |
|   |          | ii  | $g = (6400/15300)^2 \times 9.81$   | C1    |  |  |
|   |          | ii  | $g = 1.72 (N kg^{-1})$   | A1    |  |  |
|   |          | iii | Acceleration towards centre = 1.72 ms <sup>-2</sup> or centripetal force = mass of satellite × 1.72 N                    | C1    | ecf (b)(i)                                       |  |
|   |          | iii | $T^2 = 4 \times \pi^2 \times 1.53 \times 10^7 / 1.72$  | C1    |  |  |
|   |          | iii | $T = 1.87 \times 10^4 (s)$   | A1    | Allow 1.9  |  |
|   |          |     | Total  | 6     |  |  |
| 2 | а        |     | (Resultant) Force acts perpendicularly to the direction of motion  | B1    |  |  |
|   | b        | i   | $F = 5.0 \times 4.8^2 / 1.5$   | C1    |  |  |
|   |          | i   | F = 77 (N)   | A1    | Allow 76.8 (N)                                   |  |
|   |          | ii  | $\omega = v / r = 4.8 / 1.5$   | C1    | <b>Allow</b> alternative e.g. $F = m \omega^2 r$ |  |
|   |          | ii  | $\omega = 3.2 \text{ (rad s}^{-1}\text{)}$   | A1    |  |  |
|   |          |     |  |       |  |  |

| Question | Answer/Indicative content   |        | Guidance  |
|----------|---|--------|---|
| C        | * Level 3 (5–6 marks) A labelled diagram including all equipment required and a detailed description of the method leading to an appropriate analysis of data.  There is a well-developed line of reasoning which is clear and logically structured. The information presented is relevant and substantiated.  Level 2 (3–4 marks) A labelled diagram including most of the equipment required and a description of the method leading to an appropriate graph but with some misunderstanding of the relationship.  There is a line of reasoning presented with some structure. The information presented is in the most-part relevant and supported by some evidence.  Level 1 (1–2 marks) A diagram is included with most of the equipment required and a description of the method leading to an attempt of identifying an appropriate graph or relationship.  The information is basic and communicated in an unstructured way. The information is supported by limited evidence and the relationship to the evidence may not be clear. | B1 × 6 | <ul> <li>Equipment / labelled diagram(E)</li> <li>1 String / cord (passed through a tube) with bung at one end and load at other (accept a labelled diagram)</li> <li>2 Stopwatch to measure time period</li> <li>3 Suitable scale / marker to measure radius</li> <li>Method (M)</li> <li>1 Whirl bung with constant frequency and radius (in horizontal circle)</li> <li>2 Measure time for several time periods</li> <li>3 Measure radius either using cord markers or stopping the cord at the tube and measuring with a ruler</li> <li>4 Vary frequency and new radius</li> <li>Analysis (A)</li> <li>1 Expect √² ∝ r, or r α T⁻²</li> <li>2 Plot graph; e.g r against T⁻²</li> <li>3 Expect straight line through origin</li> </ul> |
|          | Total   | 11     |   |

| Q | Question  |    | Answer/Indicative content   | Marks | Guidance   |
|---|---|----|---|-------|--|
| 3 | a i A (constant) force acts at right angles to the velocity / motion (of the helium nucleus). | B1 | Note: The answer must be in terms of force and not acceleration.  Allow 'force is towards the centre of the circle'.  Not 'there is a centripetal force' - unless explained.  Not 'force is right angles to speed'.  Examiner's Comments  Candidates answered this question well, with many making reference to either a force at right angles to the velocity of the helium nucleus or a force that was directed towards the centre of the circle. |       |  |
|   |   | ii | No work done (by the force) / no acceleration in the direction of motion / no force in direction of motion  | B1    | Allow force / acceleration is at right angles to velocity / motion.  Examiner's Comments  There were some excellent answers in terms of no work done by the force acting on the helium nucleus, but equally, there were some simplistic answers such as the 'speed at A and B is the same, hence the kinetic energy remains constant'. The modal mark for this question was unexpectedly zero. |
|   | b   |    | $BQv = \frac{mv^2}{r}$ or $mv = BQr$<br>momentum = $0.20 \times 10^{-3} \times 3.2 \times 10^{-19} \times 0.15$   | C1    | Allow $v = 1.45 \times 10^3$ (m s <sup>-1</sup> ); $p = 1.45 \times 10^3 \times 6.6 \times 10^{-27}$   |

| Qı | Question |    | Answer/Indicative content  | Marks | Guidance   |
|----|----------|----|--|-------|--|
|    |          |    | momentum = $9.6 \times 10^{-24} \text{ (kg m s}^{-1}\text{)}$  | A1    | Examiner's Comments  |
|    |          |    |  |       | Most candidates successfully secured full marks. The analytical answers were wellstructured and easy to follow. Most candidates used first principles to show that the momentum was given by the equation $mv = BQr$ . A small number of candidates determined the speed $v$ of the helium nucleus first and then used $mv$ to calculate the momentum. This method was a bit longer, but the final answer was still the same. A very small number of candidates were using Coulomb's law instead of $F = BQv$ . Candidates are reminded that no marks will be awarded for substitution into incorrect equations. |
|    |          |    | Total  | 5     |  |
| 4  |          | i  | frequency is the same / not changed since (in SHM) it is independent of amplitude / (starting) displacement (AW) | В1    | Allow:since length of pendulum is unchanged  |
|    |          | ii | (maximum velocity) is reduced because amplitude / (starting) displacement is reduced (AW)                        | B1    | Allow: (Max) KE is smaller since amplitude / (starting) displacement is smaller  |
|    |          | ii | (Max) KE is reduced to one quarter / 4 times smaller   | B1    | Allow: (Max) KE is smaller because GPE is smaller  |
|    |          |    |  |       | Examiner's Comments  |
|    |          |    |  |       | This was another question requiring a reason from candidates and all too often this was not given at all or was only partially stated by the observation that the periodic time had not changed.   |
|    |          |    | Total  | 3     |  |

| Qı | Question |  | Answer/Indicative content  | Marks | Guidance                       |
|----|----------|--|--|-------|--------------------------------|
| 5  | а        |  | The force is towards the centre of the circle.   | B1    |                                |
|    |          |  | The force is perpendicular to the motion or no component of force in direction of motion; hence no work is done on the particle. | B1    |                                |
|    | b        |  | centripetal force provided by $BQv$ ; hence $\frac{mv^2}{r} = BQv$   | C1    |                                |
|    |          |  | $B = \frac{mv}{Qr} = \frac{9.11 \times 10^{-31} \times 5.0 \times 10^{7}}{1.6 \times 10^{-19} \times 0.018}$                     | C1    |                                |
|    |          |  | $B = 1.6 \times 10^{-2} (T)$   | A1    |                                |
|    |          |  | Total  | 5     |                                |
| 6  |          |  | $\lambda = \frac{\ln 2}{6600} = 1.050 \times 10^{-4}  (\text{s}^{-1})$   | C1    | Correct use of $A = \lambda N$ |
|    |          |  | $N = \frac{400 \times 10^6}{1.050 \times 10^{-4}} = 3.809 \times 10^{12}$  | C1    |                                |
|    |          |  | mass of FDG = $\frac{3.809 \times 10^{12}}{6.02 \times 10^{23}} \times 0.018 \div 0.099$   | C1    |                                |
|    |          |  | mass of FDG = $1.15 \times 10^{-12}$ (kg) or $1.2 \times 10^{-12}$ (kg)  | A1    |                                |
|    |          |  | Total  | 4     |                                |

| Qı | Question |    | Answer/Indicative content  | Marks | Guidance   |
|----|----------|----|--|-------|--|
| 7  | а        |    | $\lambda_1 = d \sin 12.5 = 4.33 \times 10^{-7} \text{ m}$<br>giving $1/d = 5 \times 10^5 \text{ or } d = 2 \times 10^{-6}$       | C1    | or $\lambda_2 = d \sin 14.0 = 4.84 \times 10^{-7} \text{ (m)}$   |
|    |          |    | $\lambda_3 = \sin 19.0/5 \times 10^5 = 6.51 \times 10^{-7} \text{ (m)}$  | A1    |  |
|    |          |    | or   |       |  |
|    |          |    | $\lambda_1 = d \sin 12.5 = 4.33 \times 10^{-7} \text{ and } \lambda_3 = d \sin 19.0$   |       |  |
|    |          |    | so $\lambda_3 = 4.33 \times 10^{-7}$ sin 19.0/sin 12.5 = 6.51 $\times 10^{-7}$ (m)   |       | or use $\lambda_2 = d \sin 14.0 = 4.84 \times 10^{-7} \text{ m sin}$<br>19.0/sin 12.5 = 0.326/0.216 = 1.50 |
|    | b        | İ  | the uncertainty in the measurement of angle is the same for all angles and the bigger the angle measured the smaller the % error | B1    |  |
|    |          | ii | n <sub>max</sub> = d sin 90  | C1    |  |
|    |          | ii | = $1/(5 \times 10^5 \times 4.33 \times 10^{-7})$ = 4.6 but n is an integer so n = 4  | A1    |  |
|    | С        | i  | 3 downward arrows correctly labelled.  | B1    | longest being 4.33 × 10 <sup>-7</sup> (m)  |
|    |          | ii | $\Delta E = hc/\lambda$  | C1    |  |
|    |          | ii | $\lambda = 6.63 \times 10^{-34} \times 3 \times 10^{8} / 4.8 \times 10^{-20} = 4.1(4) \times 10^{-6} \text{ (m)}$                | A1    |  |
|    |          | ii | region: infra red  | В1    | allow ecf if wavelength calculation incorrect.   |
|    |          |    | Total  | 9     |  |

| Qı | Question |    | Answer/Indicative content                            | Marks | Guidance  |  |
|----|----------|----|--|-------|---|--|
| 8  | а        | i  | $F = GMm/r^2 = mv^2/r$                               | C1    | where $r = 6.8 \times 10^6 \text{ m}$                                     |  |
|    |          | i  | $v = (GM/r)^{1/2} = (g/r)^{1/2}R$ (as $g = GM/R^2$ ) | C1    | N.B. some working must be shown as a                                      |  |
|    |          | i  | $v = 7.7 \text{ (km s}^{-1}\text{)}.$                | A1    | show that Q   |  |
|    |          | ii | total energy = ½mv² – GMm/r = –GMm/2r                | M1    | no ecf from (i); allow numerical values                                   |  |
|    |          | ii | $E = -gR^2m/2r = -1.2(4) \times 10^{13} (J)$         | A1    | with no algebra if clear no mark for correct value without the minus sign |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |
|    |          |    |  |       |   |  |

| Question | Answer/Indicative content   | Marks | Guidance  |
|----------|---|-------|---|
| b        | Level 3 (5–6 marks) a structured combination of at least 6 statements taken from A, B and C or A and D a combination of at least 5 statements; script of a lower quality N.B. bonus given for any of E at any level The ideas are well structured providing significant clarity in the communication of the science.  Level 2 (3–4 marks) a good combination of at least 4 statements taken from A and B or A and C or B and C or A and D a combination of at least 3 statements taken from two sections which are relevant together. There is partial structuring of the ideas with communication of the science generally clear.  Level 1 (1–2 marks) at least 2 statements from A, B, C or D which are relevant together some attempt which is related to the question The ideas are poorly structured and impede the communication of the science.  Level 0 (0 marks) Insufficient or relevant science. | B1    | <ul> <li>A initial scenario</li> <li>for circular orbit a centripetal force (of magnitude mv² / r) is required or AW in terms of accelerations</li> <li>this is provided by the gravitational force GMm/r² or G force just pulls radially inwards sufficiently to maintain orbit</li> <li>the speed in orbit v = (GM/r)¹/²</li> <li>B reverse thrust</li> <li>G force causes rocket to spiral towards Earth when rocket slowed;</li> <li>rocket speeds up in process</li> <li>v in orbit is larger when radius r is smaller; condition for faster lower orbit can be achieved or T smaller because either v is larger or r / circumference is smaller or both or 2πr/v is smaller</li> <li>C forward thrust</li> <li>when rocket speeds up with engines fired forwards G force insufficient to hold orbit so spirals to larger orbit</li> <li>slowing as it does so</li> <li>D energy approach</li> <li>some p.e. goes to k.e. when rocket is slowed as it moves towards Earth</li> <li>so v increases</li> <li>vice versa when rocket is accelerated</li> <li>E further comments</li> <li>extra corrections needed to obtain circular orbit after manoeuvre (not mentioned in passage)</li> <li>any other relevant statement not included above</li> </ul> |

| Question |  | n | Answer/Indicative content | Marks | Guidance |
|----------|--|---|---------------------------|-------|----------|
|          |  |   | Total                     | 11    |          |

| Qı | uestio | Answer/Indicative content  | Marks | Guidance   |
|----|--------|--|-------|--|
| 9  | а      | $\left(\frac{\Delta\lambda}{\lambda} = \frac{v}{c}\right)$ $\frac{\Delta\lambda}{656.3} = \frac{2.5 \times 10^5}{3.0 \times 10^8} \text{ (Any subject)}$ | C1    |  |
|    |        | Δλ = 0.55(nm)  | A1    | Note: Answer to 3 sf is 0.547 (nm) Note: $5.5 \times 10^{-10}$ on the answer line scores 1 mark  Examiner's Comments  This was another confidently tackled question. The Doppler equation was used well, with most answers for the change in wavelength given in nm. A very small number of candidates struggled to convert their answer of $5.5 \times 10^{-10}$ m into nm. |
|    | b      | $\frac{GMm}{r^2} = \frac{mv^2}{r} \text{ or } \frac{GM}{r} = v^2$  | C1    | Allow other correct methods.  Allow the following for the first two C1 marks: $F = \frac{2.0 \times 10^{30} \times (2.5 \times 10^5)^2}{0.65 \times 10^{20}}$ or $1.92 \times 10^{21}$ (N) C1 $\frac{GM \times 2.0 \times 10^{30}}{(0.65 \times 10^{20})^2} = 1.92 \times 10^{21}$ (Any subject) C1  |
|    |        | $\frac{GM}{0.65 \times 10^{20}} = (2.5 \times 10^5)^2 \text{ (any subject)}$   | C1    |  |

| Qı | uestion | Answer/Indicative content  | Marks | Guidance   |  |
|----|---------|--|-------|--|--|
|    |         | mass = $6.09 \times 10^{40}$ (kg)<br>(number of stars = $6.09 \times 10^{40}/2.0 \times 10^{30}$ ) | C1    | Allow: 2 out of 3 marks for use of 1.3 × $10^{20}$ (m); this gives an answer of 1.2 × $10^{41}$ (kg)   |  |
|    |         | number of stars = 3.0 × 10 <sup>10</sup>   | A1    | Possible ECF from incorrect mass of galaxy Allow 1 SF answer for the estimation  Examiner's Comments   |  |
|    |         |  |       | The modal mark for this question was four and about a third of the candidates scored nothing for their work. A range of methods were used to arrive at the correct answer of 3.0 × 10 <sup>10</sup> stars in the Andromeda galaxy. The most popular route was starting off with the expression |  |
|    |         |  |       | $\frac{GMm}{r^2} = \frac{mv^2}{r}$ . A significant number of candidates also successfully used the   |  |
|    |         |  |       | equation for Kepler's third law. On the whole, candidates demonstrated admirable analytical and calculator skills.   |  |
|    |         | Total  | 6     |  |  |
| 10 |         | A  | 1     |  |  |
|    |         | Total  | 1     |  |  |
| 11 |         | В  | 1     |  |  |
|    |         | Total  | 1     |  |  |

| Question |   | n   | Answer/Indicative content  | Marks | Guidance   |
|----------|---|-----|--|-------|--|
| 12       | а | i   | T W  | B1    | Both forces must be correct to score this mark.  |
|          |   |     | Correct direction and labelling for W and T                              |       |  |
|          |   | i   | Straight line for F  Correct direction <b>not</b> horizontal or vertical | B1    | Allow: Freehand sketch of <i>F</i> must lie between 15° and 75° to the horizontal to score this mark.  |
|          |   | ii  | T W  | B1    | Both forces must be correct to score this mark.  |
|          |   |     | Correct direction and labelling for W and T                              | ı     |  |
|          |   | ii  | Straight line for F  | B1    | Allow: Freehand sketch of <i>F</i> must lie between 15° and 75° to the horizontal to score this mark.  |
|          |   |     | Correct direction not horizontal or vertical                             |       |  |
|          |   | iii | T W Correct direction and labelling for W and T                          | B1    | Both forces must be correct to score this mark.  |
|          |   | iii | Straight line for F  | B1    | Allow: Freehand sketch of <i>F</i> must lie between 15° and 75° to the horizontal to score this mark.  |
|          |   |     | Correct direction <b>not</b> horizontal or vertical                      |       | Examiner's Comments  |
|          |   |     |  |       | Most candidates gave correct directions for T and W, although there were a significant number with T towards the right. Only a minority realised that the aircraft was in equilibrium and as such F must act upwards and at an angle to the right of the horizontal. |
|          | b | i   | a = T/m<br>$a = 28 \times 10^3 / 6200 (= 4.516)$                         | C1    | Must substitute to score this mark.  |
|          |   | i   | $v^2 = u^2 + 2as$<br>$56^2 = 0 + 2 \times 4.516s$ (any subject)          | C1    | Answer to 3 sf = 347 (m).  Allow: max 2 marks if v is not squared but correct formula was quoted. [Expect s = 6.2 (m)]   |
|          |   |     |  |       |  |

| Ques | tion | Answer/Indicative content   | Marks | Guidance   |
|------|------|---|-------|--|
|      | i    | s= 350 (m)  | A1    | Allow: $Fs = \frac{1}{2} mv^{2} $ [C1] $28 \times 10^{3} s = \frac{1}{2} \times 6200 \times 56^{2} $ [C1] (any subject) $s = 350 $ (m) [A1] Allow:   |
|      |      |   |       | Ft = $mv$<br>t = 12.4 (s) [C1]<br>$s = \frac{1}{2}vt = \frac{1}{2} \times 56 \times 12.4$ [C1]<br>s = 350 (m) [A1]   |
|      |      |   |       | Examiner's Comments  |
|      |      |   |       | Well answered by all but a small number of candidates who, having determined the time correctly, proceeded to calculate the distance using the product of final velocity and time.   |
|      | ii   | Air resistance / drag / friction acts on aircraft decreasing either the net forward force or the acceleration | M1    | Not: 'slowing the aircraft down'.  |
|      | ii   | Fs = ΔKE so reduced force must act over a longer distance to produce enough kinetic energy for take-off OR    | A1    | Allow word equation.  Note: This mark cannot be given if the previous (M1) mark has not been scored.   |
|      |      | $v^2 = (u^2) + 2as$ so reduced acceleration<br>means longer distance to reach take-off                        |       | Examiner's Comments  |
|      |      | speed.  |       | Most candidates mentioned air resistance and friction but only the minority of very good candidates continued the discussion to give a mathematical reason for the increase in distance. A clear example of the need to read the question carefully. |
| С    | i    | L cos35° =6200 × 9.81   |       | Allow: Use of 9.8  |
|      | i    | $L = \frac{6200 \times 9.81}{\cos 35^{\circ}}  \text{OR}  L = 7.42 \times 10^{4}$                             | M1    |  |
|      |      |   |       |  |

| Question | Answer/Indicative content                                    | Marks | Guidance  |
|----------|--|-------|---|
| i        | $L = 7.4 \times 10^4 (\text{N})$                             | A0    | Note: There is no mark for the answer as it is given in the question. Marks in 'Show' questions are for the working.  |
|          |  |       | Examiner's Comments   |
|          |  |       | Most candidates handled the calculation well and showed their working clearly.  |
| ii       | $L \sin 35^\circ = mv^2/r$                                   | C1    |   |
| ii lii   | $r = \frac{6200 \times 86^2}{7.4 \times 10^4 \sin 35^\circ}$ | C1    | Possible ecf from (c)(i).   |
| ii       | i  | A1    | Correct answer to 3 sf = 1.08 × 10 <sup>3</sup> (m).  Allow: 1 mark for using cos 35° instead of sin 35°. Expect gives an answer of 760 (m).  Allow: 2 marks for correct working using v = 56 (m s <sup>-1</sup> ) Expect an answer of <i>r</i> = 460 (m).  No marks for using tan 35° or for omitting a trig function.  Examiner's Comments  Candidates used a range of approaches to the trigonometry required in this more searching calculation, and although most were successful, a disappointing proportion used the raw value of L from (i) rather than the horizontal component. |
| d i      | Indication at 'top' of circle (by eye)                       | B1    | the nembers of mperiors.  |
| i        | 0 (N)  | B1    | Examiner's Comments  The vast majority of candidates showed their understanding of this aspect of motion in a vertical circle by scoring the first mark for the position of A. Many went on to score the mark for the vertical contact force, although there were a variety of incorrect answers from weaker candidates, the most common of which was the weight.   |

| Question | Answer/Indicative content   | Marks | Guidance   |
|----------|---|-------|--|
| ii       | P is not the resultant force OR Resultant force must be towards centre of circle so P must have a component acting vertically upwards, equal in magnitude to W (AW) | B1    | Allow: (Horizontal) component of <i>P</i> provides centripetal acceleration and vertical component of <i>P</i> is equal to weight. (AW)  Examiner's Comments  Only the best candidates were able to give clear, correct answers to this stretch and challenge question. There were some excellent answers including diagrams to illustrate the situation. One worrying aspect evident in many incorrect answers was the number of candidates who thought that there was no resultant force acting on the aircraft at the point B. The somewhat ambiguous phrase 'balancing forces' was |
|          | Total   | 14    | frequently seen where 'zero resultant force' was more appropriate.   |

| Q  | uestio | n  | Answer/Indicative content   | Marks                | Guidance   |
|----|--------|----|---|----------------------|--|
| 13 | а      |    | arrow down through centre of ball labeled weight or W or mg or 1.2 N  | B1                   | zero if any other arrows or forces present  Examiner's Comments There were some carelessly drawn arrows on the diagram but otherwise this was done well. There were some arrows labelled <i>centripetal force</i> .  |
|    | b      | i  | (horizontally) $mv^2/r$ (or $mr\omega^2$ ) = T $\sin\theta$ and (vertically) W or $mg = T \cos\theta$ (tan $\theta = v^2/rg$ or $rw^2/g$ ) tan $\theta = 0.045 \times 4 \times 9.87 \times 2.2 / 9.81$ or $0.48 / 1.2$ (= 0.40) $\theta = 22^\circ$ | M1<br>A1<br>A0       | accept figures in place of algebra, $r = 0.045 \text{ m}$ $v = 0.42 \text{ m s}^{-1} \omega = 3\pi \text{ rad s}^{-1}$ ; $r\omega^2 = 4.0 \text{ m s}^{-2}$ ; $W = 1.2 \text{ N}$ and $m = 0.12 \text{ kg}$ and $mr\omega^2 = 0.48 \text{ N}$ accept labelled triangle of forces diagram N.B. this is a <i>show that Q</i> ; sufficient calculation must be present to indicate that the candidate has not worked back from the answer   |
|    |        | ii | $k = (mg / x_0 = 1.2 / 0.050) = 24 (N m^{-1})$<br>$(T = mg / cos \theta = kx giving)$<br>x = 1.2 / 24 cos 22<br>x = 0.054 (m )  | C1<br>C1<br>A1       | examiner's Comments About half of the candidates completed the angle calculation successfully with a slightly smaller number finding the correct extension of the string.  |
|    | С      |    | $(y = \frac{1}{2}gt^2 =) 0.18 = 0.5 \times 9.81 \times t^2$ giving $t = 0.19$ (s) $(x = vt =) 0.42 \times 0.19 = 0.08$ (m) distance $= \sqrt{(r^2 + x^2)} = \sqrt{(0.0020 + 0.0064)} = 0.092$ (m)   | C1<br>C1<br>C1<br>A1 | alt: projectile motion: $x = vt$ , $y = \frac{1}{2}gt^2$<br>$y = \frac{1}{2}g(x / v)^2$<br>ecf (b)i for $v$ ; $x^2 = 2yv^2/g$<br>$= 2 \times 0.18 \times 0.42^2/9.81$<br>Examiner's Comments<br>About half of the candidates found the time for the ball to fall to the bench. Most then managed to find the horizontal distance from the point of release, but half forgot that the point of reference in the question was the centre of rotation so failing to complete the calculation. |

| Qı | Question |  | Answer/Indicative content  | Marks | Guidance   |
|----|----------|--|--|-------|--|
|    | d        |  | T increases <b>or</b> string stretches <b>or</b> angle θ increases | M1    |  |
|    |          |  | to provide / create a larger centripetal force                     | A1    | allow mv²/r or mrω² in place of <i>centripetal</i> force causality must be implied to gain the A mark  Examiner's Comments About half of the candidates appreciated that the tension in the string increased or that the angle of the string to the vertical increased. Most answers gave the impression that the <i>centripetal force</i> was a real force rather than its provision being necessary for the ball to follow a circular path |
|    |          |  | Total  | 12    |  |

| Question |    | Answer/Indicative content   | Marks | Guidance  |  |
|----------|----|---|-------|---|--|
| 14       | i  | Horizontal arrow pointing to the right.                             | B1    | Judgement by eye  |  |
|          |    |   |       | Examiner's Comments  The examiners were quite lenient in this series in terms of the precise direction of the arrow, which should point towards the                         |  |
|          |    |   |       | centre of Mars.   |  |
|          | ii | $2.14 \times 10^3 = \frac{2 \times \pi \times 9380 \times 10^3}{T}$ | C1    |   |  |
|          |    | $T = 2.75 \times 10^4 \text{ (s)}$                                  | A1    | Allow 2SF answer Note: 2.75 × 10 <sup>n</sup> scores 1 mark.  |  |
|          |    |   |       | Examiner's Comments   |  |
|          |    |   |       | Around four fifths of candidates got this right. Those that did not either poorly converted the radius from km or used the area rather than the circumference of the orbit. |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |
|          |    |   |       |   |  |

| Question | Answer/Indicative content  | Marks          | Guidance  |
|----------|--|----------------|---|
| iii      | $\frac{GMm}{r^2} = \frac{mv^2}{r}  \text{or}  v^2 = \frac{GM}{r}$ $(2.14 \times 10^3)^2 = 6.67 \times 10^{-11} \times M/9380 \times 10^3$ $M = 6.44 \times 10^{23} \text{ (kg)}$ | C1<br>C1<br>A1 | Allow ecf of answer for T from (a)(ii)  Allow 2 SF answer Note: Use of 2.8 × 10 <sup>4</sup> seconds gives 6.3 × 10 <sup>23</sup> (kg) for 3 marks.  Alternative Method for C1C1  • M = 4π <sup>2</sup> R <sup>3</sup> /(T <sup>2</sup> G) (Databook formula re–arranged with M as subject) • M = 4π <sup>2</sup> (9380 × 10 <sup>3</sup> ) <sup>3</sup> /((2.75 × 10 <sup>4</sup> ) <sup>2</sup> × 6.67 × 10 <sup>-11</sup> ) (i.e. M as subject)  Note: In alternative method, PoT error forgetting km–>m conversion gives 6.46 × 10 <sup>14</sup> (kg) for 2 marks.  Examiner's Comments  Many candidates successfully used the equation for Kepler's Third Law, which is encouraging. A quicker route was to find the Phobos's acceleration (from v <sup>2</sup> /r) and equating that to the gravitational field strength at Phobos from Mars (GM <sub>mars</sub> /r <sup>2</sup> ) and then rearranging to find the mass of Mars. |
|          | Total  | 6              |   |

| Question | Answer/Indicative content  | Marks | Guidance   |
|----------|--|-------|--|
| 15 a     | $T = 60/1600 \text{ or } T = 3.75 \times 10^{-2} \text{ (s)}$<br>$(v = \pi \times 0.50/3.75 \times 10^{-2})$ | C1    | Allow: $f = 26.7$ or $\frac{1600}{60}$ (Hz) or $\omega = 168$ (s <sup>-1</sup> )   |
|          | speed = 42 (m s <sup>-1</sup> )  | A1    | Note: v must be to 2 or more SF  |
|          | uncertainty = 3 (m s <sup>-1</sup> )   | A1    | Note: uncertainty must be to 1 SF Allow: ecf on candidate's value for speed i.e. uncertainty = candidate's value / 16 (to 1 SF)  Allow for 2 marks max: 84 ± 5 (m s <sup>-1</sup> )  Examiner's Comments  About half of the candidates got this item right or provided clear working to show where they were going. There was much confusion about which quantity was which. 1600 revolutions per minute refers to the frequency of the rotation, not the angular speed, angular frequency or the speed itself.  The percentage error of the frequency was 6.25%, prior to rounding. Some candidates multiplied this by their value for the speed to get the correct absolute uncertainty, although good practice is to round uncertainties to 1 SF. |

| Qu | Question |  | Answer/Indicative content          | Marks | Guidance   |
|----|----------|--|------------------------------------|-------|--|
|    | b        |  | $m\sqrt{r} = mg$ or $\sqrt{r} = g$ | C1    | Allow: $v^2/r = a \text{ and } a = g \text{ or } mv^2/r = ma \text{ and } a = g$<br>Allow: any subject   |
|    |          |  | $v^2 = 9.81 \times 0.25$           | C1    | Allow: any subject   |
|    |          |  | $v = 1.6 \text{ (m s}^{-1})$       | A1    |  |
|    |          |  |                                    |       | <b>Note:</b> qualified 2.21 (ms <sup>-1</sup> ) scores 2 marks.  |
|    |          |  |                                    |       | Examiner's Comments  |
|    |          |  |                                    |       | This question was answered well by those above the mean result. When the machine is switched off, the clothes are still in circular motion and at point B, the resultant force is still the weight of the clothes plus the normal contact force. |
|    |          |  |                                    |       | This means at the critical speed when the clothes fall off at point B, the centripetal force will equal the weight of the clothes, since the question states that the normal contact force is zero.  |
|    |          |  | Total                              | 6     |  |

| Question | Answer/Indicative content  | Marks | Guidance   |
|----------|--|-------|--|
| 16 i     | (For circular orbit) centripetal force provided by gravitational force (of attraction) | M1    |  |
|          | provided by gravitational force (of  | A1    | Examiner's Comments  Only a minority of candidates related the gravitational force between the stars to the centripetal force required for circular motion to occur. This candidate has written the perfect answer (exemplar 5).  There were two popular insufficient answers; that if the stars were not diametrically opposite they would collide and that the centre of mass of the system had to be at the centre of the orbit.  Exemplar 5  **That grantetinal free 15 about the control of the c |
|          |  |       |  |

| Question | Answer/Indicative content   | Marks | Guidance   |
|----------|---|-------|--|
| ii       | $T = 20.5 \times 86400 \ (= 1.77 \times 10^6 \ s) \ and \ R = 1.8 \times 10^{10} \ (m)$ | C1    | values of T and R scores first mark; both incorrect 0/3  |
|          | $m = 16 \times \pi^2 \times (1.8 \times 10^{10})^3 / G \times (20.5 \times 86400)^2$    | C1    | correct substitution allowing $\pi^2$ and G<br>$m = 16 \times 9.87 \times 1.8^3 \times 10^{30}/6.67 \times 10^{-11} \times 1.8^2 \times 10^{12}$   |
|          | giving $m = 4.4 \times 10^{30}$ so $m = 2.2 \text{ M}_{\odot}$                          | A1    | using 2R gives $35.2 \times 10^{30}$ = 17.6 M $_{\odot}$ or using T = 1 day gives $1850 \times 10^{30}$ = 930 M $_{\odot}$ award 2/3   |
|          |   |       | Examiner's Comments  |
|          |   |       | This question tested the candidates' ability to interpret and substitute data into an elaborate formula and then evaluate it. The most common error was to write the formula with the correct substitutions but then to omit the square symbol against T. Candidates should be encouraged to consider whether their answers are reasonable before moving on to the next question. In the calculation (exemplar 6) shown here, is it possible that these stars could be four million times the mass of the Sun? The correct answer of 2.2 Sun masses seems very plausible and should give candidates confidence.  |
|          |   |       | Exemplar 6   |
|          |   |       | $ \frac{1 \text{ day} = 884008}{M_{\odot} = 2.0 \times 10^{30} \text{kg}} = \frac{16 \pi^2 \times (1.8 \times 10^{10})^3}{6.67 \times 10^{-11} \times (20.5 \times 8.64 \times 10^{41})} = \frac{7.795 \text{ m} \times 10^{36} \text{ kg}}{2 \times 10^{30}} = \frac{3.8977 \text{ m} \times 10^6}{2 \times 10^{30}} = \frac{3.9 \times 10^6}{10^6} = 3.$ |

| Quest | ion | Answer/Indicative content  | Marks | Guidance  |
|-------|-----|--|-------|---|
|       | iii | $v = 2\pi R/T = 2 \times 3.14 \times 1.8 \times 10^{10} / 1.8 \times 10^{6}$<br>(giving $v = 6.3$ or $6.4 \times 10^{4}$ ) | C1    | do not penalise repeated error for R or T   |
|       |     | $\Delta \lambda = (v/c)\lambda = (6.3/3) \times 10^{-4} \times 656 = 0.14$ (nm)  | A1    | ecf for incorrect v, gives $\Delta \lambda = v \times 2.2 \times 10^{-6}$ $\Delta \lambda = 0.28$ for 2R; $\Delta \lambda = 2.9$ for 1 day and $\Delta \lambda = 5.7$ for both incorrect  Examiner's Comments  Most of the higher performing candidates completed this problem successfully. Two common errors among the remainder were to equate the formula for central force gravitational potential energy ( <i>GMm/r</i> ) to kinetic energy to find a value for the speed of the stars and to rewrite incorrectly metres in powers of 10 in nanometres. |
|       |     | Total  | 7     |   |

| Question | Answer/Indicative content                            | Marks | Guidance   |
|----------|--|-------|--|
| 17 i     | $F = (mv^2/r =) 8.0 \times 1.5^2/2.0$<br>F = 9.0 (N) | C1 A1 | Allow answer to 1s.f.  |
|          |  |       | Examiner's Comments  Question 4(b)(ii) proved very difficult and highlighted poor understanding of circular motion. Almost all candidates described the centripetal force as an additional force that had appeared out of nowhere. This centripetal force 'pulled the suitcase inwards' (or, in some cases, outwards) or 'balanced the frictional force' or 'added to the frictional force' and so on.   |
|          |  |       | Exemplar 5  At It the lag is using in an arrangemental correct acting on the well as with priction and the format. I notice to keeple large in equilibrium, grition has to increase and these to learn a the second of the central grows and these to learn and the control of the central force, row acts on the suitcase. The forces F and R have to adjust in order to keep the suitcase in equilibrium. They have not realised that the suitcase is no longer in equilibrium horizontally but is accelerating. This means that the available forces have to adjust in order to provide a resultant force towards the centre of the circle, while still balancing vertically.  Exemplar 6 |

| Question | Answer/Indicative content | Marks | Guidance   |
|----------|---------------------------|-------|--|
|          |                           |       | The suities. is now accelering towards the center of the sensitive. This means here is a conference of the sensitive. The sensitive is a composed to the left so Frust means to the lef |

| Question |   | n  | Answer/Indicative content  | Marks          | Guidance  |
|----------|---|----|--|----------------|---|
|          |   | ii | <ul> <li>Suitcase accelerates / changes its velocity / (constantly) changes direction / has a resultant force acting on it / is no longer in equilibrium</li> <li>The resultant force must act (horizontally) towards centre of circle / to the left</li> <li>The centripetal force can only be provided by (an increase in) F</li> <li>Increased vertical component of F means the vertical component of R must decrease (in order to balance W)</li> <li>So R must decrease</li> </ul> | B1 x 4 A0      | Any answer that mentions <b>centrifugal</b> force scores $0/4$ <b>Ignore</b> any statement that treats the centripetal force as an extra force <b>Allow</b> net or unbalanced or total for resultant throughout <b>or</b> $F\cos 30^\circ - R\sin 30^\circ$ increases (from 0 to $9.0 (N)$ ) / the (magnitude of the) horizontal component of $F$ must exceed the (magnitude of the) horizontal component of $R$ <b>not</b> a resultant force acts towards <b>Y</b> e.g. Friction is the only force able to provide the centripetal force / only F has a component to the left <b>Allow</b> $F$ provides the centripetal force <b>Not</b> the horizontal force must increase / increases <b>or</b> $F\sin 30^\circ + R\cos 30^\circ = W/W$ is the vector sum of $F$ and $R/W = (F^2 + R^2)\frac{1}{2}$ (and $F$ increases while $W$ remains constant) Total |
|          |   |    | Total  | 6              |   |
| 18       | а |    | $F = m\omega^2 r$ and $\omega = 2\pi f$ $kmg = m\omega^2 r$ Clear algebra leading to $f^2 = \left(\frac{gk}{4\pi^2}\right) \times \frac{1}{r}$   | M1<br>M1<br>A1 | Allow $F = mv^2/r$ and $v = 2\pi fr$<br>Allow this mark for $kmg = mv^2/r$  |
|          | b |    | <i>y</i> -intercept = – 0.45   | C1             | Allow ± 0.05  |
|          |   |    | $\frac{1}{2}\lg\left(\frac{gk}{4\pi^2}\right) = -0.45$ $\left(\frac{gk}{4\pi^2}\right) = 10^{-0.9}$  | C1             | Allow attempt at calculating y-intercept using gradient and a point on the line.  |
|          |   |    | $k = \frac{0.126 \times 4 \times \pi^2}{9.81}$   | C1             | Not e <sup>-0.9</sup> wrong physics   |
|          |   |    | k = 0.51   | A1             | Allow k in range 0.48 to 0.63  Note Answer must be to 2 SF  |
|          |   |    | Total  | 7              |   |

| Question | Answer/Indicative content  | Marks | Guidance   |
|----------|--|-------|--|
| 19 a     | There is no contact force between the astronaut and the (floor of the) space station (so no method of measuring / experiencing weight) | B1    | Allow astronaut and the space station have same acceleration (towards Earth) / floor is falling (beneath astronaut)  Examiner's Comments  Misconception  Experiencing weightlessness is not the same as being in freefall  There was a lack of understanding of the nature of feeling weightless. The sensation of 'weightlessness' is a lack of the physiological sensation of 'weight'. The skeletal and muscular systems are no longer in a state of stress. This sensation is caused by a lack of contact forces as a result of the ISS and the astronaut experiencing the same acceleration.  Common incorrect responses included:  • the astronaut is weightless because he is falling  • there is no resultant force on the astronaut  • gravity is too weak to have any effect on the astronaut  • the ISS orbits in a vacuum where there is no gravity. |

| $(gr^2 = \text{constant so}) \ g \times (6.78 \times 10^6)^2 = 9.81 \\ \times (6.37 \times 10^6)^2$ $g = 8.66 \ (\text{N kg}^{-1})$ Allow rounding of final answer to 2 SF i.e. $8.7 \ (\text{N kg}^{-1})$ $Examiner's Comments$ The simplest method here was to use the fact that $g$ is inversely proportional to $r^2$ , so $gr^2 = \text{constant}$ . If this was not used, a value for the mass of the Sun had to be calculated, which introduced a further step Candidates who omitted this calculation and used a memorised value of the Sun's mass instead were unable to gain full marks, because they invariably knew it to 1 s.f. only, whereas 3 were required.  Errors occurred when candidates used the incorrect distance in the formula for $g$ . Common errors included:  • forgetting to square the radius • using the Earth's radius rather than the orbital radius of the satellite • calculating $(6.37 \times 10^6 + 4.1 \times 10^6)$ incorrectly. | Question | Answer/Indicative content   | Marks | Guidance   |
|---|----------|---|-------|--|
| $T = 5.5 \times 10^3 \text{ s} (= 92 \text{ min})$  |          | or ISS orbital radius $R = 6.78 \times 10^6$ (m) or $g \propto 1/r^2$ ( $gr^2 = \text{constant so}$ ) $g \times (6.78 \times 10^6)^2 = 9.81 \times (6.37 \times 10^6)^2$ $g = 8.66$ (N kg <sup>-1</sup> ) | C1    | Allow rounding of final answer to 2 SF i.e. 8.7 (N kg <sup>-1</sup> )  Examiner's Comments  The simplest method here was to use the fact that <i>g</i> is inversely proportional to <i>r</i> <sup>2</sup> , so <i>gr</i> <sup>2</sup> = constant. If this was not used, a value for the mass of the Sun had to be calculated, which introduced a further step. Candidates who omitted this calculation and used a memorised value of the Sun's mass instead were unable to gain full marks, because they invariably knew it to 1 s.f. only, whereas 3 were required.  Errors occurred when candidates used the incorrect distance in the formula for <i>g</i> . Common errors included:  • forgetting to square the radius  • using the Earth's radius rather than the orbital radius of the satellite  • calculating (6.37 × 10 <sup>6</sup> + 4.1 × 10 <sup>5</sup> ) incorrectly. |

| Question | Answer/Indicative content   | Marks | Guidance  |
|----------|---|-------|---|
| С        | $\frac{1}{2}Mc^{2}(\frac{1}{2}N_{A}mc^{2}) = \frac{3}{2}RT$                             | C1    |   |
|          | =   | C1    | or $\frac{1}{2}mc^2 = \frac{3}{2}kT$ or $c^2 = 3kT/m$   |
|          | $c^2 = 3 \times 8.31 \times 293 / 2.9 \times 10^{-2} = 2.52 \times 10^{5}$              | A1    | or $c^2 = 3 \times 1.38 \times 10^{-23} \times 6.02 \times 10^{23} \times 293/2.9 \times 10^{-2} = 2.52 \times 10^5$  |
|          | $\sqrt{c^2} = 500 \text{ (m s}^{-1})$   | A0    | not $(7.7 \times 10^3 / 15) = 510 \text{ (m s}^{-1})$<br>Examiner's Comments  |
|          | $(=7.7 \times 10^3 / 15)$   |       |   |
|          |   |       | The success in this question depended on understanding the meaning of the term <i>m</i>   |
|          |   |       | in the formula $\frac{1}{2}m\overline{c^2} = \frac{3}{2}kT$ given in the Data, Formulae and Relationship booklet. A significant number of candidates took $m$ to be the mass of one mole (the molar mass, $M$ ) whereas $m$ is actually the mass of one molecule. Candidates who used the                                 |
|          |   |       | formula $\frac{1}{2}M\overline{c^2} = \frac{3}{2}RT$ were usually more successful because the molar mass had been given in the question stem.   |
| d        | power reaching cells (= $IA$ ) = 1.4 × 10 <sup>3</sup> × 2500 = 3.5 × 10 <sup>6</sup> W | C1    | mark given for multiplication by 0.07 at any stage of calculation   |
|          | power absorbed = $0.07 \times 3.5 \times 10^6 = 2.45 \times 10^5 \text{ W}$             | C1    | (90 - 35 =) 55 minutes using $T = 90$   |
|          | cells in Sun for (92 – 35 =) 57 minutes   | C1    | minutes  ECF value of T from b(ii)  |
|          | average power = $57/92 \times 2.45 \times 10^5 = 1.5 \times 10^5$ (W)                   | A1    | $55/90 \times 2.45 \times 10^5 = 1.5 \times 10^5$ (W) using T = 90 minutes  |
|          |   |       | Examiner's Comments   |
|          |   |       | Although this question looked daunting, it was actually quite linear and many candidates who attempted it were able to gain two or three marks even if they did not eventually get to the correct response. Candidates who set out their reasoning and working clearly were more liable to gain these compensatory marks. |
|          | Total   | 13    |   |